Device for Testing the Fatigue Life of Composite Structural Elements of Vehicles

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BIOGRAPHICAL NOTES
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KEY WORDS
Fatigue tests; Polymer composite, Motor vehicle.

ABSTRACT
The paper presents the device of the fatigue tests in the complex load states. The measuring system can measure and record the temperature of the elements tested, the number of fatigue cycles, twisting and bending angles of the sample and its load. The device is used to test the fatigue strength of elements of the carrying structures of the vehicles and machines cophasally loaded with the bending and twisting moments.

1. INTRODUCTION
Each load-carrying structure put on the dynamic load is subject to the fatigue effect. This is involved with the generation and development of fatigue cracks which lead to weakening and often destruction of the structure. The effect of fatigue is very common in the light, strained structures such as the load-carrying structures of automotive vehicles. Contemporary trends to reduce the energy consumption in vehicles while ensuring the high levels of exploitation parameters result in the increasing use of polymer composites for construction of the load-carrying structure. This forces the search for solution to the problems associated with determining the fatigue life of
structures made from these materials. Typical fatigue calculations are performed based on the data of element loads and allowable stresses (the Wohler curve for the harmonic loads). Due to the stochastic nature of the vehicle loads the direct use of such runs to assess the durability of the structure is not possible. So the method of loads reduction for the stochastic runs is used and the Wohler curve is applied. Assuming a suitable hypothesis of fatigue damage culmination the fatigue life of the element can be defined. The accuracy of these calculations depend on the accuracy of the adoption of the correct hypothesis of damage culmination, accuracy of determination of the substitute spectrum of loads and fatigue characteristics of the material. Particularly troublesome is to determine the fatigue strength, the limiting number of fatigue cycles and the Wohler curve exponent. Determination of these parameters, using laboratory testing of the samples of polymer composites, does not produce satisfactory results. For these reasons, the fatigue tests are increasingly being conducted on the real structures or large elements thereof. Such tests should take into account the impact of the type of load on the fatigue life of the designed element. Elements of the vehicle body are mostly bent in the vertical and horizontal planes and twisted. The local load of vehicle subassemblies has less influence on the fatigue life. This paper presents a research stand with the measuring system allowing to conduct the testing of fatigue of elements of machines and vehicles in complex state of loads.

2. Construction and Operation of the Fatigue Device

It was assumed that the device should enable the fatigue testing of samples and real elements in a complex state of loads. This state is most common in elements of the carrying structures of automotive vehicles. After review of fatigue testing machines [1,3] the torsion-bending test resonance device with semicircular handles has been chosen. The device allows burdening of a sample with the bending and twisting moments acting cophasally. This case is considered to be the most unfavorable load of the carrying elements of vehicle. Schemes of similar devices have been presented in this paper [2]. The device was built to test the vehicle carrying elements made of polymer composites. In order to force the loads, the inertial vibrator driven by three-phase AC motor controlled by a frequency converter was chosen. The maximum length of the element tested is 550 mm, the frequency of forced loads is up to 50 Hz. The angle of deflection of inertial disks is approximately.

The overall construction of the device is shown in Fig. 1. The element tested is fixed in holders mounted on guides of the semicircular forcing elements. The guides are rigidly connected with the inertial disks. On the periphery of the disks the sectional weights are mounted. The inertial vibrator driven by an electric motor is attached to the active disk. The horizontal component of the centrifugal force of the rotating vibrator masses (4, fig.1) induces the angular vibration of the active disk. As a result of these vibration the element tested is burden.

![Fig. 1: Scheme of the fatigue device; 1 - motor, 2 - main shaft, 3 - v-belt, 4 and 5 - vibrator weights, 6 i 10 - inertial disks, 7 - handles, 8 - semicircular guides.](image)
show in Fig. 2.

![Fig. 2](image)

Fig. 2: Distribution of the external moment depending on the angle of the sample setting.

In cases where the bending rigidity and torsion rigidity are equal, which is extremely rare, the moments distribution is as follows:

\[ M_s = M \sin \alpha \]  \hspace{1cm} (1)

\[ M_c = M \cos \alpha \]  \hspace{1cm} (2)

If \( k_s \neq k_c \), then [2]:

\[ M_s = \frac{M}{k_1} k_c \sin \alpha \]  \hspace{1cm} (1)

\[ M_c = \frac{M}{k_1} k_c \cos \alpha \]  \hspace{1cm} (3)

\[ k_1 = k_c \sin^2 \alpha + k_c \cos^2 \alpha \]  \hspace{1cm} (4)

\[ k_c = \frac{E}{l} + \frac{2l_k}{l_k} \]  \hspace{1cm} (5)

\[ k_s = \frac{Gl_k}{l} \]  \hspace{1cm} (6)

where: \( l \) - measuring length of the sample, \( l_k \) - length of the sample mounting terminals, \( I_n \) - moment of inertia of the torsion bounded, \( I_p \) - moment of inertia of the measured part of the sample with respect to axis "z", \( k_s \) - moment of inertia of the sample terminals with respect to axis "z".

The external moment \( M \) can be calculated from the relationship:

\[ M = k_s \cdot (\varphi_1 - \varphi_2) \]  \hspace{1cm} (7)

The angle of torsion \( \varphi \) can be calculated by solving the system of equations:

\[ \begin{cases}
I_1 \frac{d^2 \varphi_1}{dt^2} + c_1 \frac{d\varphi_1}{dt} + (k_1 + k_2) \varphi_1 - k_1 \varphi_2 = M_{01} \\
I_2 \frac{d^2 \varphi_2}{dt^2} + c_2 \frac{d\varphi_2}{dt} - k_1 \varphi_1 + (k_1 + k_2) \varphi_2 = 0
\end{cases} \]  \hspace{1cm} (8)

Assuming a solution in the form:

\[ \varphi_1 = a_1 \sin (\omega t + \varphi_{10}), \varphi_2 = a_2 \sin (\omega t + \varphi_{20}), \varphi = \varphi_1 - \varphi_2 \]  \hspace{1cm} (9)

\[ \varphi = A_1 \sin (\omega t + \varphi_0), A_1 = \sqrt{c_1 + c_2}, \tan \varphi_0 = \frac{c_1}{c_2} \]  \hspace{1cm} (10)

\[ c_1 = a_1 \sin \varphi_{10} - a_2 \sin \varphi_{20}, c_2 = a_1 \cos \varphi_{10} - a_2 \cos \varphi_{20} \]  \hspace{1cm} (11)

\[ a_1 = \sqrt{A_1^2 + B_1^2}, a_2 = \sqrt{A_1^2 + B_1^2}, \tan \varphi_0 = \frac{B_1}{A_1}, \tan \varphi_0 = \frac{B_1}{A_1} \]  \hspace{1cm} (12)

\[ A_1 = \frac{M_0}{A_1^2 + B_1^2}, A_2 = \frac{M_0}{A_1^2 + B_1^2} \]  \hspace{1cm} (13)

\[ B_1 = \frac{M_0}{A_1^2 + B_1^2}, B_2 = \frac{M_0}{A_1^2 + B_1^2} \]  \hspace{1cm} (14)

\[ A = [(k_1 + k_2 - \omega^2 I_1)k_1 + k_2 - \omega^2 I_1] - k_1 - \omega^2 c_1 c_2] \]  \hspace{1cm} (15)

\[ B = [c_1 (k_1 + k_2 - \omega^2 I_1) + c_1 (k_1 + k_2 - \omega^2 I_1)] \]  \hspace{1cm} (16)

The moment acting on the inertial disk can be calculated from the relationship:

\[ M_{01} = M_0 \cos \omega t \]  \hspace{1cm} (17)

Fig. 3: Dynamic model of the device.

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I_2 \frac{d^2 \varphi_2}{dt^2} + c_2 \frac{d\varphi_2}{dt} - k_1 \varphi_1 + (k_1 + k_2) \varphi_2 = 0
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\[ \varphi = A_1 \sin (\omega t + \varphi_0), A_1 = \sqrt{c_1 + c_2}, \tan \varphi_0 = \frac{c_1}{c_2} \]  \hspace{1cm} (10)

\[ c_1 = a_1 \sin \varphi_{10} - a_2 \sin \varphi_{20}, c_2 = a_1 \cos \varphi_{10} - a_2 \cos \varphi_{20} \]  \hspace{1cm} (11)

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\[ B_1 = \frac{M_0}{A_1^2 + B_1^2}, B_2 = \frac{M_0}{A_1^2 + B_1^2} \]  \hspace{1cm} (14)

\[ A = [(k_1 + k_2 - \omega^2 I_1)k_1 + k_2 - \omega^2 I_1] - k_1 - \omega^2 c_1 c_2] \]  \hspace{1cm} (15)

\[ B = [c_1 (k_1 + k_2 - \omega^2 I_1) + c_1 (k_1 + k_2 - \omega^2 I_1)] \]  \hspace{1cm} (16)

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Fig. 4: Centrifugal force on the vibrator; \( m \) - mass of the weight, \( P_o \) - centrifugal force, \( \nu \) - frequency of the exciting force.
While the centrifugal force and the moment in the oscillator are described by the equations:

\[ P_0 = mr^2 \nu^2 \] and moment \( M_0 = P_0 \cdot R \] \hspace{1cm} (18)

The frequency of free vibration, assuming the same bearings of the disks and identical inertial disks, can be calculated from the relationship:

\[ \omega_{1/2} = \frac{n_1 + n_2}{2I} \pm \sqrt{\frac{1}{4} \left( \frac{n_1 + n_2}{I} \right)^2 - \frac{n_1 n_2 - k_1^2}{I^2}} \] \hspace{1cm} (19)

where:

\[ n_1 = -lh^2 + k_3 + k_1, \quad n_2 = -lh^2 + k_1 + k_2 \]

3. The measuring system

The measuring system can measure and record the temperature of the element tested, the number of the fatigue cycles, the twisting and bending angles of the sample and its load. For registration of the measurements signals the specifically developed measuring system was used. The schematic of the measurement system is shown in Fig. 5.

![Fig. 5: Microprocessor based measuring system for recording signals during fatigue testing: PC – a control computer, SP – a microprocessor recorder, KS – a signal converter, T1-T4 – silicon sensors of temperature, L1-L2 – potentiometric sensors measuring the angle of deflection, I1-I2 photo-optical sensors to control the cycles of deflection.](image)

The main elements of the measuring system are: PC – a control computer, a microprocessor-based recorder (SP) and a signal converter (KS). The measuring system enables simultaneous, multi-channel measurement and recording of the following values:

- temperatures of the four semiconductor temperature sensors,
- angular deflection from two potentiometric transducers of displacement,
- number of deflection cycles from two photo-optical sensors.

The presented configuration of the measurement signals in the first turn allows to determine the self-excited temperature adopted as a criterion of the fatigue destruction. On the surface of the sample tested three silicon sensors were placed. The forth sensor, as a compensation one, is used to measure the ambient temperature. Sensors with a special construction of the signal converter enable the temperature measurement with resolution of 0.01°C. The adopted solution provides measurement and recording of even minimal changes of temperature on the surface of the sample tested. The idea of measuring the twist angle \( \alpha \) of the sample is shown in Fig. 6.

![Fig. 6: Measurement of the angle of torsion of the sample: 1 - movable disk of the forcing unit, 2 - potentiometric sensor of displacement, 3 - pillar.](image)

The signal obtained directly at the output of the potentiometric converter of displacement (2) is the signal that is information on linear displacement \( \Delta 1 \) of the mandrel (slider) of the potentiometer forced by the angular movement \( \Delta \alpha \) of the support coupled with that mandrel in “a floating” system (3). In order to measure and record the angle of torsion \( \alpha \) of the sample, the appointment and maintaining of the processing characteristics were done at the beginning which are described with the relationship:

\[ \Delta \alpha = f(\Delta U) \] \hspace{1cm} (20)

The accepted concept of construction of the measuring system of the open configuration enables, in a simple manner, connecting of additional
measuring transducers, eg. strain gauges to measure the deformation in the attachment points of the element tested. In Fig. 7 the arrangement of transducers are schematically shown.

![Fig. 7: Placement of the measuring sensors: 1 - temperature sensors, 2 - sensors of the angular displacements of disks, 3 - sensors of the fatigue cycles counter.](image)

### 4. Research Possibilities

The fatigue device inductor is powered by a three-phase AC motor through a belt transmission. The control of rotational speed is achieved by the frequency inverter type RN82 LUMEL. The forced loads frequency can be adjusted by the change of the motor rotations, while the moment of loading of the element tested can be regulated by changing the mass of the weights attached to the vibrator disks. Reactive guide in its lower part is connected to the base of the device with an elastic connector. The rigidity of the connector can be adjusted. Similarly, the active disk is connected to the base by coil springs and pillars. Using the changes in the stiffness of connectors of both disks and their moments of inertia the dynamic model of the device can be changed from the dual mass system with one natural frequency to the system with two frequencies of natural vibrations. Below, in the Fig. 8, 9 and 10 the possibilities of loading the element tested are shown. Depending on the angle of inclination of the sample, various possibilities of its load are achieved. From loading with torque moment only through a complex state of loading (bending and twisting moments) to loading solely with the twisting moments). The device allows therefore for conducting the high-cycle fatigue tests of samples and construction elements.

![Fig. 8: Loading with the twisting moment Ms.](image)

![Fig. 9: Cophasal loading with the bending $M_g$ and twisting $M_s$ moments.](image)

![Fig. 10: Loading with the bending moment $M_g$.](image)

![Fig. 11: View of the research stand with a composite sample.](image)

### 5. Conclusions

The paper presents the stand of the fatigue tests in the complex load states. The measuring system can measure and record the temperature of the elements tested, the number of fatigue cycles, twist-
ing and bending angles of the sample and its load. The device is used to test the fatigue strength of elements of the carrying structures of the vehicles and machines cophasally loaded with the bending and twisting moments. It is possible to equip the device with stereoscopic microscope with a camera recording with high resolution (e.g. Moticam 1000) for observation and measurement of fatigue crack propagation.

6. References