**New Method of Residual Stress Evaluation and its Advantages in Comparison with More Common Hole-drilling Method**

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**KEY WORDS**

Ring-Core, hole-drilling method, residual stresses.

**ABSTRACT**

Residual stress evaluation in constructions and mechanical parts is a necessary task in every modern industrial factory. Right evaluated changes in lifetime and loading con-

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**BIOGRAPHICAL NOTES**

Ing. František Menda (1989) successfully accomplished the high school with base on mathematics. Then he began studies at the Faculty of Mechanical Engineering of the Technical University of Košice. He graduated with honours a bachelor-degree study in Mechatronics in 2010 and continued an engineer degree study in same program. He defended his diploma thesis “Design of the conception for contactless control of air knives with drives for zincify production line no.3” in 2012 and accomplished this study with an honours. Nowadays, he is a PhD. student of Mechatronics and is concentrating on measuring of residual stress by Ring-core method.

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Ing. Patrik Šarga, PhD. (1979) He graduated in „Automation and Control in Mechanical Engineering“ at Technical University of Košice in 2002. He was an internal PhD. student at the Department of Applied Mechanics and Mechatronics and in 2005 he defended his dissertation thesis in field of mechatronics. Nowadays he works as an assistant on the Department of Applied Mechanics and Mechatronics at the Faculty of Mechanical Engineering at Technical University of Košice. He is co-author of three books of lecture notes and more than 50 publications in journals and conference proceedings at Slovakia and abroad, e.g. Engineering Failure Analysis, Metalurgija. He has worked on several grant projects, research tasks and many projects solved for industry realized on the department.
ditions could save amount of money and increase the human safety. The Department of Applied Mechanics and Mechatronics has a long tradition in developing and practical usage of semi-destructive methods for determining residual stresses. Especially by using hole-drilling method and recently also Ring-Core method. Main characteristics and comparison of both methods with emphasis on Ring-Core analysis are discussed in this article.

1. Introduction

The lifetime prediction of every designing construction could be determined analytically using adequate equations from the theory of material strength by considering geometric parameters of the object and applied loads and deformations. During manufacturing procedures and machining processes like e.g. casting, stamping, grinding, shot peening or welding occur inside the materials specific state of stresses, which affect the total load capacity and the lifetime of investigated objects. Such inside stresses are called residual stresses and exist even without any external load. They also occur during production cycle, which could be extremely dangerous and unexpected. Insufficient attention devoted to the matter of residual stresses could in worst case lead to the destruction and costly repairs or even to danger of a human life. Therefore it is necessary to determine the magnitude, direction and sense of residual stresses acting in potentially risky parts of investigated object.

1.1 Semi-destructive measuring methods

Recently, there are various types of measuring methods for determining residual stresses inside the objects of interest. Generally they can be classified as follows: optical, acoustic, mechanical, roentgen, numerical methods.

This article deals more about mechanical methods. Mechanical methods evolved from rather cumbersome destructive methods, in which the tested object was totally destroyed, to semi-destructive methods, easily applicable in both laboratory and industrial conditions. Main advantage of semi-destructive method is its minimal effect on the working cycle and lifetime of tested object after measuring. The most common semi-destructive methods for residual stress determination are:

- **hole-drilling method**,  
- **Ring-Core method**.

2. Hole-drilling Method

The hole-drilling method technique involves monitoring the change in stresses (or strains) produced when a hole is drilled into a component with residual stress. The dimensions of drilled hole are very small: both diameter and depth 1÷4mm. Therefore this method is only semi-destructive, the produced hole may be insignificant or repaired after testing. The change in strain may be measured on the top of specimen using photoelasticity, brittle-coating or electrical strain gages. Blind rather than through holes are used and reading of strain change is in various depths to assess the variation with depth. This allows us to create an idea of residual stress distribution along the specimen thickness. The hole is drilled into small depths because the residual stresses usually show up near the surface in form of cracks [1].

![Fig. 1: Hole-drilling method.](image)

For measuring revealed strain values on top of the specimen’s surface we can use three basic types of strain gage rosettes defined by ASTM E 837 [2].

**Fig. 2: Types of strain gage rosettes [2].**

**Type A:**  
- **Strain gage rosette for general using, e.g. RY61 made by HBM (Fig. 2a),**  
- **Dimensions:**  
  - $a = 1.5 \text{mm}$,  
  - $b = 0.8 \text{mm}$,  
  - $d = 12 \text{mm}$,  
  - resistance 120 Ω.
Type B:
■ All grids are placed in one direction (Fig. 2b),
■ This strain gage rosette is used for drilling near obstacle.

Type C:
■ It is used for measuring strains with high sensitivity and in cases of high temperature stability (Fig. 2c),
■ Rosette has three pairs of grids placed opposite each other which are connected to half bridge circuits.

The hole-drilling method is recently easily applicable and pretty precise method for evaluating residual stresses, defined by the standard ASTM E837-08 [3]. The Department of Applied Mechanics and Mechatronics has researched and developed the practical usage of this method for few decades. The most common device for experimental testing is RS200 (Fig. 3). This device consists of a simple stand for centering. Because it has no actuator, it requires a drill for making a hole. Static strain gage system P3500 connected with computer enables reading data values from strain gage rosette.

More sophisticated system is MTS 3000 produced by SINT (Fig. 4). It is an automatic measuring system which is equipped by high-speed pneumatic turbine. The accuracy of positioning and centering is increased by build in microscope.

3. Ring-Core method

Ring-Core method is another semi-destructive method using for residual stress evaluation inside the material. This method improves some weaknesses of the hole-drilling method, but it brings more damage to the tested specimen. Similarly as in hole-drilling method, the principle is about attaching the special strain gage rosette to the specimen’s surface. Instead of drilling a hole through the middle of the rosette, an annular notch is milled around the strain gage. This creates the isolated core, inside which the residual strains (stresses) relax. The dimensions of milled notch are: 14mm inner and 18mm outer diameter. The process of stress relieving is divided into small step increments up to maximum milling depth 5mm. Subsequently the distributions of residual stresses along the milled depth at specific investigated place are determined.

XY51:
■ It is used when directions of principal stresses are known (Fig. 6a),
■ Dimensions: $a=5\text{mm}$, $b=2.5\text{mm}$, $c=12\text{mm}$, electrical resistance $350\Omega$.

RY51:
■ It is used with unknown directions of principal stresses (Fig. 6b),
■ Dimensions: $a=5\text{mm}$, $b=2.5\text{mm}$, $c=12\text{mm}$, electrical resistance $350\Omega$. 
The Department of Applied Mechanics and Mechatronics owns fully automated measuring system MTS 3000 Ring-Core from SINT company. The system is designed for constant measuring and data evaluation during Ring-Core measuring procedure. Measuring string consists of mechanical unit for milling an annular notch, electronic control unit, digital strain gage amplifier (e.g. HBM Spider 8.30 or Quantum X) and computer with measuring and post-processing software. The mill positioning towards the strain gage rosette is provided by webcam in connection with utility Eyeshot.

Data cables from strain gage rosette are lead through the hollow mill and subsequently through the whole machine body. Such solution allows continuous data acquisition without the need of disconnecting and re-connecting cables. Especially problems with continuous data transfer during the precisely centered milling around the rosette slowed down the progress of the Ring-Core method. The Ring-Core method recently outmatches experimentally easier applicable hole-drilling method.

Another way of performing a hole/notch is by using a laser cut. The results are satisfied according to the created shape of a hole, but unsatisfied according to the temperature influencing around the hole. The laser beam of low intensity is not useful. Plastic deformations occurring near the hole boundaries could be microscopically detected. For that reason it is not recommended to use laser beam in combination with the methods used for measuring residual stresses.

Though both methods are similar (both methods consists of material removal in place of strain gage and subsequent measurement of deformation released from the nearby material), the most significant difference is in the shape of opening.

Hole-drilling method requires drilling a hole with the diameter 1÷4mm through the middle of the rosette up to the depth equals to the hole diameter. By using Ring-Core method instead of drilled hole, annular notch with the diameter 14mm is milled up to maximum depth 5mm, with the rosette placed in the middle on top of created core. Such measurement procedure release higher amount of deformations and the data signal is of the higher order. Ring-Core method is also not sensitive to temperature gradients near the milled notch.

The Ring-Core method is also more sufficient in cases of milling into coarse-grained materials like castings or welds. Measured objects should be more massive thus the annular notch is not close to the sharp geometric boundaries of the specimen.
To curved surfaces of investigated object could also make difficulties with right placing, measuring and evaluating according standard set of calibration coefficients. Milling to very thin specimen, respectively opening through whole thickness is by the nature of the method not possible.

Generally, the material removal procedures are carried in places, where during operating conditions the resulting opening will not act as an impermeable stress concentrator, or it can be removed by further processing operation.

4.2 Disadvantages of the Ring-Core method

The most significant disadvantages of the Rig-Core method in comparison with the hole-drilling method come from insufficient method development and no standardization of measuring and evaluation procedure. They are:

- the necessity to determine unique set of calibration coefficients (for uniform state of stress) respectively calibration factors (for non-uniform state of stress) in the dependence on mechanical parameters of measured material, geometric characteristics of the specimen and creating core, total milling depth, number and distribution of the steps and type of the strain gage rosette,
- limited applicability of the method and the necessity of respecting the factors affecting the accuracy of measurement,
- the possibility of affecting the state of stress inside the material by inadequate place of measurement.

5. Evaluation of residual stresses components by the Ring-Core method [5], [6]

The input parameters for residual stress determination in the dependence on the milling depth are:

- material properties: Young’s modulus E and Poisson’s number μ,
- three function curves of relieved strains (ε₁, ε₂, ε₃) in the dependence on the changing depth, obtained from three measuring grids of strain gage rosette.

There are three common calculation methods for processing the input data:

- incremental method, suitable for uniform residual stress field,
- differential method, suitable for the easy view on uniform residual stress distribution along the specimen depth,
- integral method, suitable for non-uniform residual stress field.

5.1 Incremental method

Incremental method is based on the following assumptions:

- the strain (stress) increment is constant at each step of milling procedure,
- state of stress in particular step is not affected by the previous steps,
- stress in vertical direction (perpendicular to the strain gage surface) is negligible according to the strain values in plane of the strain gage rosette.

Principal residual stresses σ₁ and σ₂ are subsequently calculated according the following equations:

\[
\sigma_1 = \frac{E}{K_1 - \mu^2 K_2^2} \left( K_1 \frac{d\varepsilon_1}{dz} + \mu K_2 \frac{d\varepsilon_2}{dz} \right)
\] (1)

\[
\sigma_2 = \frac{E}{K_1 - \mu^2 K_2^2} \left( K_1 \frac{d\varepsilon_2}{dz} + \mu K_2 \frac{d\varepsilon_1}{dz} \right)
\] (2)

Where \( K_1 \) and \( K_2 \) are calibration coefficients.

5.2 Differential method

Special type of incremental method is the differential method. For evaluating by this method there is needed to mill the final depth only in two steps. Subsequently there are only two sets of measured strain values. Therefore the size of difference \( \Delta z \) consists of difference of two different milled depths \( z_i \) and \( 2z_i \).

\[
\Delta z = 2z_i - z_i = z_i, pre z_i = 1, 2, 3, 4 \text{ mm} (3)
\]

Residual stresses are calculated according the following equations:

\[
\sigma_1 = \frac{E}{K_1 - \mu^2 K_2^2} \cdot \frac{1}{\Delta z} \left( K_1 \Delta \varepsilon_1 + \mu K_2 \Delta \varepsilon_2 \right)
\] (4)

\[
\sigma_2 = \frac{E}{K_1 - \mu^2 K_2^2} \cdot \frac{1}{\Delta z} \left( K_1 \Delta \varepsilon_2 + \mu K_2 \Delta \varepsilon_1 \right)
\] (5)

with:

\[
\Delta \varepsilon_1 = (\varepsilon_1)_2 - (\varepsilon_1)_1
\] (6)

\[
\Delta \varepsilon_2 = (\varepsilon_2)_2 - (\varepsilon_2)_1
\] (7)

5.3 Integral method

Unlike the previous evaluation methods, integral method is based on assumption that each drilling step is influenced by the previous one. Therefore this method is suitable for calculating of non-uniform...
form residual stresses. Principal stresses $\sigma_{ij}$, $\sigma_{2j}$ in the j-th layer of milled notch, as a product of $i=1,..n$ step increment are calculated:

$$\sigma_{1j} = \frac{1}{4} \left[ \frac{\varepsilon_{aij} + \varepsilon_{cij}}{A_{ij}} + \frac{\varepsilon_{aij} - \varepsilon_{cij}}{B_{ij}} \right]$$  \hspace{1cm} (8)$$

$$\sigma_{2j} = \frac{1}{4} \left[ \frac{\varepsilon_{aij} + \varepsilon_{cij}}{A_{ij}} - \frac{\varepsilon_{aij} - \varepsilon_{cij}}{B_{ij}} \right]$$  \hspace{1cm} (9)$$

Where $\varepsilon_{aij}$, $\varepsilon_{cij}$ are strains read from strain gage rosette in principal directions and $A_{ij}$, $B_{ij}$ are calibration factors for integral evaluation method.

The disadvantage of integral method is complicated process of determining the calibration factors. Determining of set of both calibration coefficients for incremental method and calibration factors for integral method is researched by using simulations and finite elements method.

6. An Experimental Example of Measuring Residual Stresses by the Ring-Core Method in Comparison to the Hole-drilling Method

For verification of a new method in direct comparison with the hole-drilling method an experimental testing on appropriate specimen was done. To be sure of initial state of stress ($\sigma_1=45\text{MPa}$, $\sigma_2=0\text{MPa}$) an annealed specimen (without any residual stress) of the thickness 10mm was chosen and loaded by the loading machine. Material parameters of the tested specimen were: $E=210\text{ GPa}$, $\mu=0.3$. At the middle of the specimen the hole-drilling method using system RS200 and at close place the Ring-Core method were used for residual stress measurement (Fig.8).

The acquired results of evaluated residual stresses by both methods are in Fig.9 and Fig.10.

7. Conclusion

In the article there were described two semi-destructive methods for evaluating residual stresses inside the materials, hole-drilling method and Ring-Core method. The Department of Applied Mechanics and Mechatronics has a long tradition of developing and practical usage of the hole-drilling method, which is recently most common semi-destructive method due to its easy applicability and standardized evaluation procedure. Ring-Core measuring method is in terms of usage and applicability relatively young method, which development is a part of research also at our department.

The primary task is to determine the universal set of calibration coefficients (factors) suitable for particular material characteristics and measuring strain gage rosette. The determination of these coefficients is provided using finite elements method in simulation software Solidworks and Ansys. Next, necessary step in development of the method is subsequent verification of acquired coefficients. Verification experiment has to be done on the specimen without any residual state of stress (annealed specimen), experimentally loaded using external loading device. Such procedure allows us to directly compare applied load with the experimentally evaluated state of stress.

After series of verification experiments with considering adequate influencing factors it will be pos
possible to measure and evaluate any type of residual stress inside the investigated specimen by using system MTS 3000 Ring-Core.

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9. References